

Factoring Quadratics $ax^2 + bx + c$

(1) Factor the common factor of coefficients if possible and to change the coefficient of x^2 to a positive integer.

(2) Find two integers with **Product= a . c** and **Sum= b**.

Let them be **d** and **e**.

(3) Use the following table to find the common factors of columns and rows:

		↑	↑
←	ax^2		dx
←	ex		c

Example: Factor $2x^2 - 7x + 6$

(1) The coefficients 2, -7 and 6 have no common factors and the coefficient of x^2 is positive.

(2) Find two integers with **Product** = $2 \times 6 = 12$ and **Sum** = -7.

The integers are **-3** and **-4**.

(3) Use the following table to find the common factors of columns and rows:

So the factor is **$(2x-3)(x-2)$**

	$2x$	-3
$x \leftarrow$	$2x^2$	$-3x$
$-2 \leftarrow$	$-4x$	6

Example: Factor $12x^2 - 24x - 15$

(1) The common factor of coefficients 12, -24 and -15 is 3. Thus:

$$12x^2 - 24x - 15 = 3(4x^2 - 8x - 5). \text{ Now factor } 4x^2 - 8x - 5.$$

(2) Find two integers with **Product** = $4 \times (-5) = -20$ and **Sum** = -8.

The integers are **+2** and **-10**.

(3) Use the following table to find the common factors of columns and rows

So the factor is **$3(2x+1)(2x-5)$**

	$2x$	$+1$
$2x \leftarrow$	$4x^2$	$2x$
$-5 \leftarrow$	$-10x$	-5

Example: Factor $-x^2 + x + 6$

(1) The coefficients -1, +1 and 6 have no common factors, but the coefficient of x^2 is negative. Thus we write:

$$-x^2 + x + 6 = -(x^2 - x - 6). \text{ Now factor } x^2 - x - 6.$$

(2) Find two integers with **Product** = $1 \times (-6) = -6$ and **Sum** = -1.

The integers are **+2** and **-3**.

(3) Use the following table to find the common factors of columns and rows

So the factor is **$-(x-3)(x+2)$**

	x	-3
x ←	x^2	$-3x$
$+2$ ←	$+2x$	-6