

## Integral Formulas

$$\textcircled{1} \int x^r dx = \frac{1}{r+1} x^{r+1} + C \quad -1 \neq r$$

$$\textcircled{2} \int x^{-1} dx = \int \frac{1}{x} dx = \ln |x| + C$$

$$\textcircled{3} \int \frac{1}{ax+b} dx = \frac{1}{a} \ln |ax+b| + C$$

$$\textcircled{4} \int \frac{f'(x)}{f(x)} dx = \ln |f(x)| + C$$

$$\textcircled{5} \int K dx = Kx + C$$

$$\textcircled{6} \int K f(x) dx = K \int f(x) dx$$

$$\textcircled{7} \int (f(x) + g(x)) dx = \int f(x) dx + \int g(x) dx$$

$$\textcircled{8} \int a^x dx = \frac{1}{\ln a} a^x + C$$

$$\textcircled{9} \int e^x dx = e^x + C$$

$$\textcircled{10} \int \sin(ax+b) dx = -\frac{1}{a} \cos(ax+b) + C$$

$$\textcircled{11} \int \cos(ax+b) dx = \frac{1}{a} \sin(ax+b) + C$$

$$\textcircled{12} \int \tan(ax+b) dx = \frac{1}{a} \ln |\sec(ax+b)| + C$$

$$\textcircled{23} \text{ Substitution: If } \int f(x) dx = g(x), \text{ then } \int f(u) du = g(u)$$

$$\textcircled{24} \text{ By Parts: } \int U dV = U \cdot V - \int V du$$

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### Trigonometric Substitutions:

$$\frac{a^2 - u^2}{\quad} \quad u = a \sin \theta$$

$$\frac{a^2 + u^2}{\quad} \quad u = a \tan \theta$$

$$\frac{u^2 - a^2}{\quad} \quad u = a \sec \theta$$

$$\textcircled{13} \int \cot(ax+b) dx = \frac{1}{a} \ln |\sin(ax+b)| + C$$

$$\textcircled{14} \int \sec(ax+b) dx = \frac{1}{a} \ln |\sec(ax+b) + \tan(ax+b)| + C$$

$$\textcircled{15} \int \csc(ax+b) dx = \frac{1}{a} \ln |\csc(ax+b) - \cot(ax+b)| + C$$

$$\textcircled{16} \int \sec^2(ax+b) dx = \frac{1}{a} \tan(ax+b) + C$$

$$\textcircled{17} \int \csc^2(ax+b) dx = -\frac{1}{a} \cot(ax+b) + C$$

$$\textcircled{18} \int \sec(ax+b) \cdot \tan(ax+b) dx = \frac{1}{a} \sec(ax+b) + C$$

$$\textcircled{19} \int \csc(ax+b) \cdot \cot(ax+b) dx = -\frac{1}{a} \csc(ax+b) + C$$

$$\textcircled{20} \int \frac{dx}{\sqrt{a^2-x^2}} = \sin^{-1}\left(\frac{x}{a}\right) + C$$

$$\textcircled{21} \int \frac{dx}{a^2+x^2} = \frac{1}{a} \tan^{-1}\left(\frac{x}{a}\right) + C$$

$$\textcircled{22} \int \frac{dx}{x\sqrt{x^2-a^2}} = \frac{1}{a} \sec^{-1}\left(\left|\frac{x}{a}\right|\right) + C$$